

## Chapter 2

# APPLICATION AND CASE STUDIES

### Outline

- SBR Semi-Batch Reactor System: Monitoring
- Batch Pulp Digester: Inferential Kappa Number Control
- Nylon 6,6 Autoclave: Monitoring & Inferential Control of Quality Variables
- Continuous Pulp Digester: Inferential Kappa Number Control

## 2.1 PCA MONITORING OF AN SBR SEMI-BATCH REACTOR SYSTEM

### 2.1.1 INTRODUCTION

#### Background

- In operating batch reaction systems, certain *abnormalities* (e.g., increased feed impurity level, catalyst poisoning, instrumentation malfunctioning) develop that eventually throw the quality completely off spec.
- It is desirable to catch these incipient faults quickly so that the problem can be rectified.
- It is desirable not to rely on lab measurements for this purpose since this will introduce significant delays.

#### Key Idea

- Use more easily measured process variable trends to classify between normal batches and abnormal batches.
- The key problem is to extract out the key identifying features (*finger prints*) from trajectories of large amount of variables.

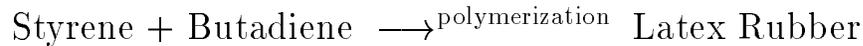
#### Appication

- An SBR Polymerization Reactor.

## 2.1.2 PROBLEM DESCRIPTION

### Process / Problem Characteristics

- Reaction:

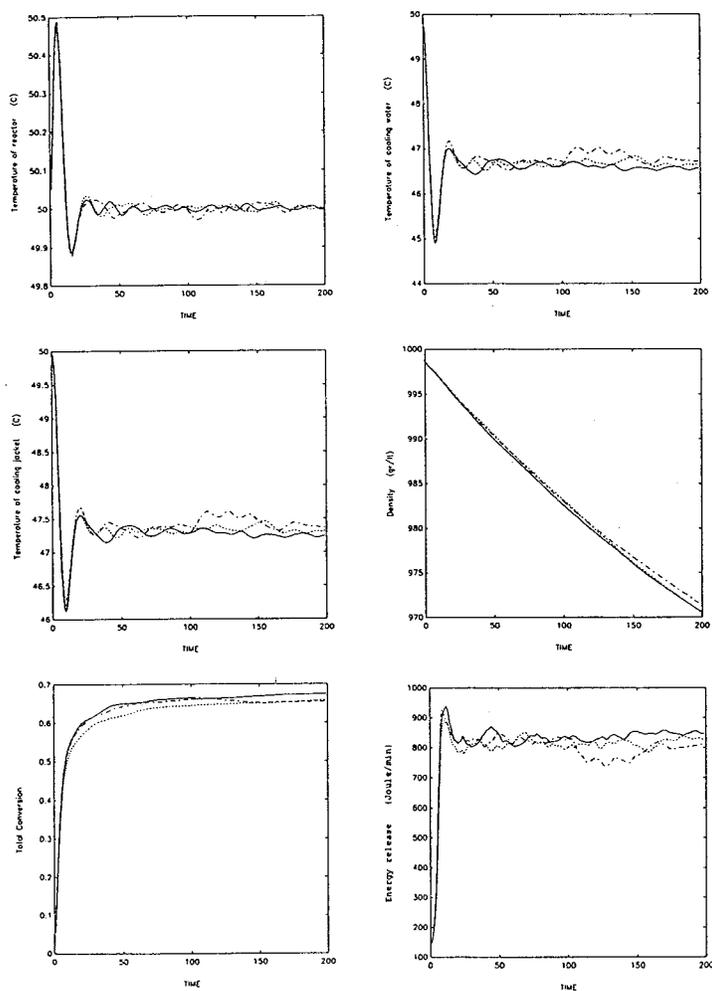


- Emulsion Polymerization
- The reactor is initially charged with seed SBR particles, initiator, chain-transfer agent, emulsifier, a small amount of styrene and butadiene monomers.
- Batch duration is 1000 minutes.
- The following measurements are available with 5 minute interval:
  - flow rates of styrene
  - flow rates of butadiene
  - temperature of feed
  - temperature of reactor
  - temperature of cooling water
  - temperature of reactor jacket
  - density of latex in the reactor
  - total conversion (an estimate)
  - instantaneous rate of energy release (an estimate)

### Available Data

- 50 batch runs with typical random variations in base case conditions (such as initial charge of seed latex, amount of chain transfer agent and level of impurities).

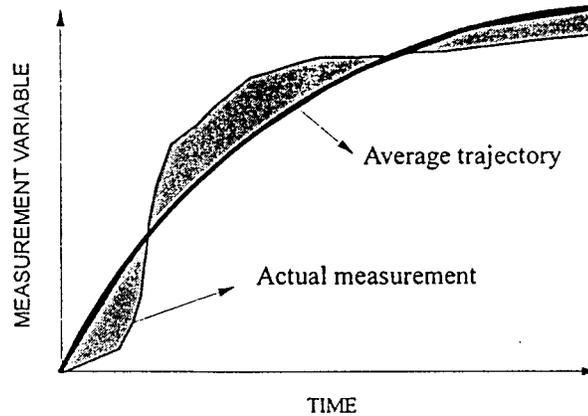
- Two additional batches with “unusual disturbances.”
  - impurity of 30% above that of the base case was introduced in the butadiene feed at the beginning of the batch.
  - impurity of 50% above that of the base case was introduced in the butadiene feed at the halfway mark.



### 2.1.3 RESULTS

#### End-Of-Batch Principal Component Analysis

- Establish the mean trajectory for each variable and compute the deviation trajectory.



- Normalize each variable with its variance.
- Perform “lifting”, that is, stack all the trajectories into a common vector to obtain a single vector  $\mathcal{Y}$  for each batch. Then, form a matrix  $Y$  by aligning  $\mathcal{Y}$  for the entire 50 batches.

Note the dimension of  $\mathcal{Y}$  is  $9 \times 200$ . Clearly there are only a few modes of variations in this vector.

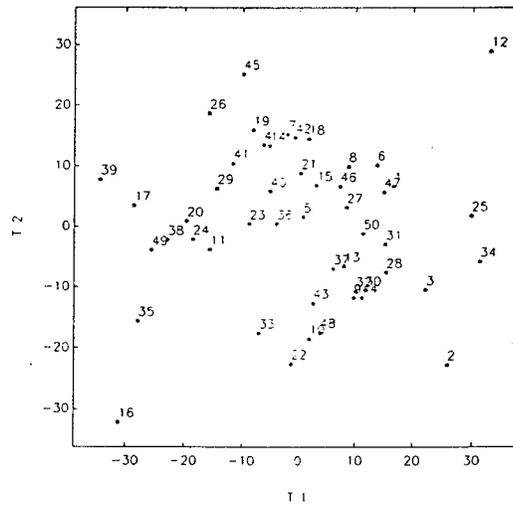
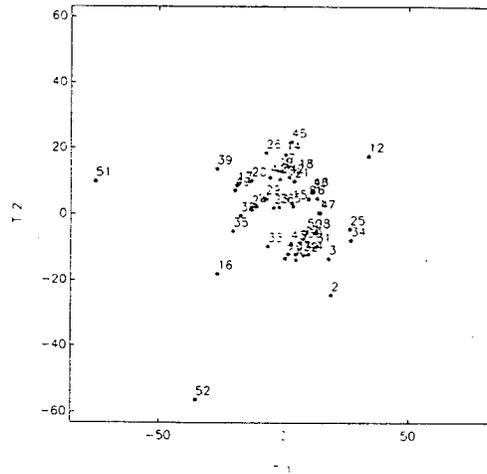
- Determine the principal component directions (eigenvectors of  $Y$  with significant eigenvalues). Three components were judged to be sufficient.

$$Y = \left[ \begin{array}{ccc|cccc} v_1 & v_2 & v_3 & v_4 & \cdots & v_{1800} \end{array} \right] \left[ \begin{array}{c|ccc} \sigma_1 & & & \\ & \sigma_2 & & \\ & & \sigma_3 & \\ \hline & & & \sigma_4 \\ & & & \ddots \\ & & & & \sigma_{1800} \end{array} \right] \left[ \begin{array}{c} v_1^T \\ v_2^T \\ v_3^T \\ \hline v_4^T \\ \vdots \\ v_{1800}^T \end{array} \right]$$

- Compute the principal component score variables for each batch:

$$t_i(j) = v_i^T \mathcal{Y}(j), \quad i = 1, \dots, 3 \quad j = 1, \dots, 50$$

The first two P.C. scores for the 50 batches and the two bad batches are plotted below:



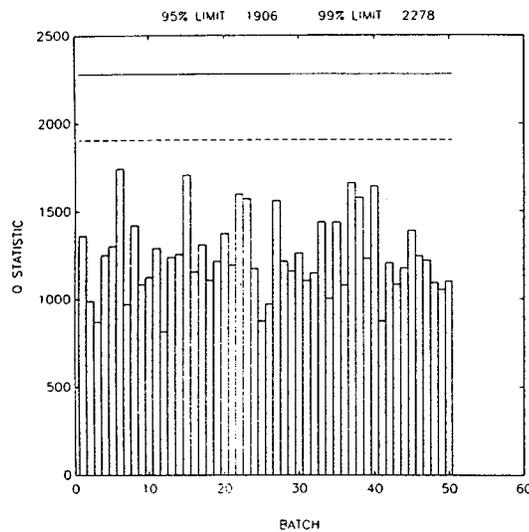
Compute the covariance matrix (diagonal)  $R_t$  for the P.C.'s. Establish the 95% and 99% confidence limits (ellipses) for the P.C.'s.

One can also use Hotelling Statistics:

$$D = t^T R_t^{-1} t \frac{N(N - m)}{m(N^2 - 1)} \sim F_{m, N-m}$$

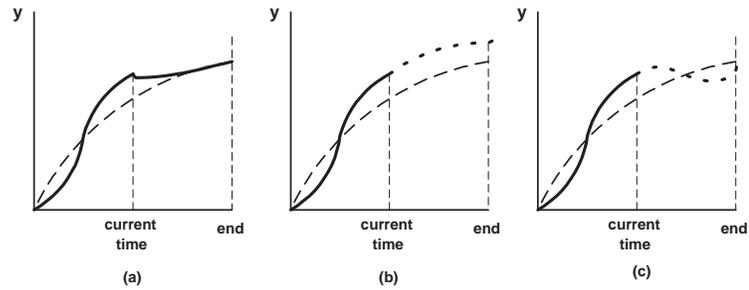
Here  $t = [t_1, t_2, t_3]^T$  and  $N = 50$  and  $m = 3$ .

- Compute the residuals and establish the 95% and 99% confidence limits for the square sum (assuming normality of the underlying distribution). The SPE (sum of the squares of the residuals) for each batch is plotted against the confidence limits:



## During-Batch Principal Component Analysis

- The main issue in applying the PC monitoring during a batch is what to do with the missing future data.



Handling missing measurement

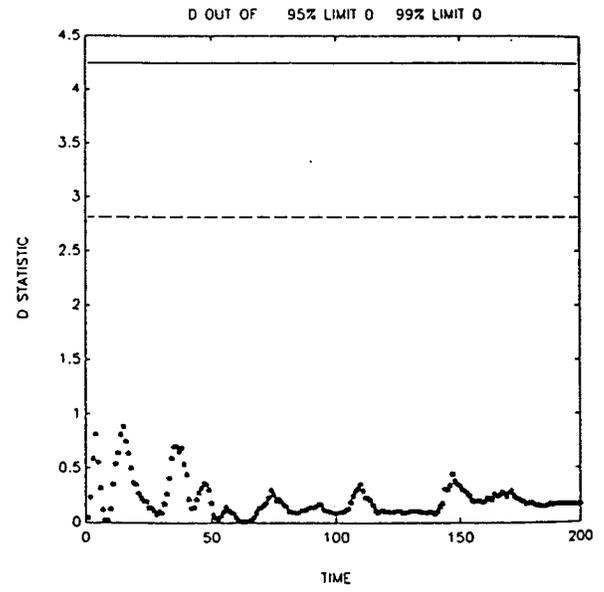
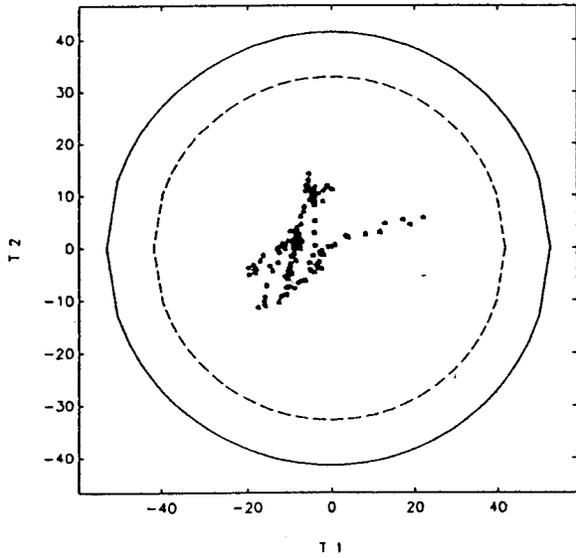
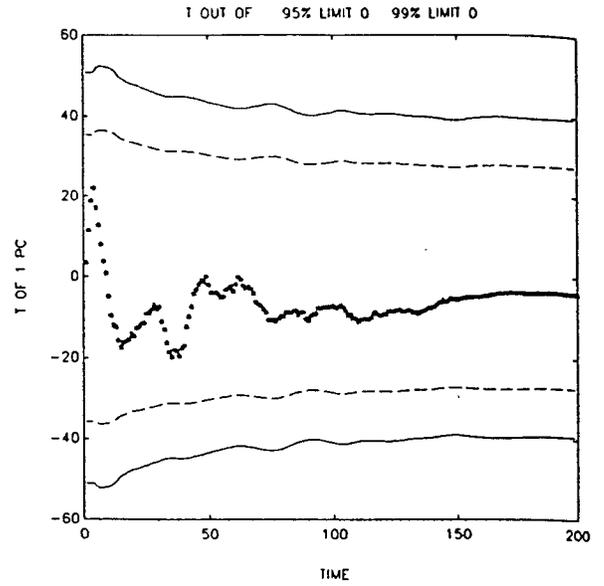
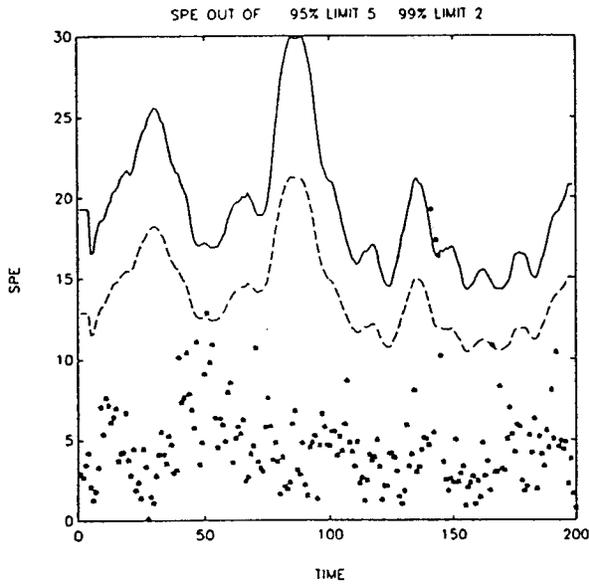
Options are:

- Assume for all the variables that the future deviation will be zero.
- Assume for each variable that the current level of deviation will continue until the end of batch.
- Use statistical correlation to estimate the future deviation.

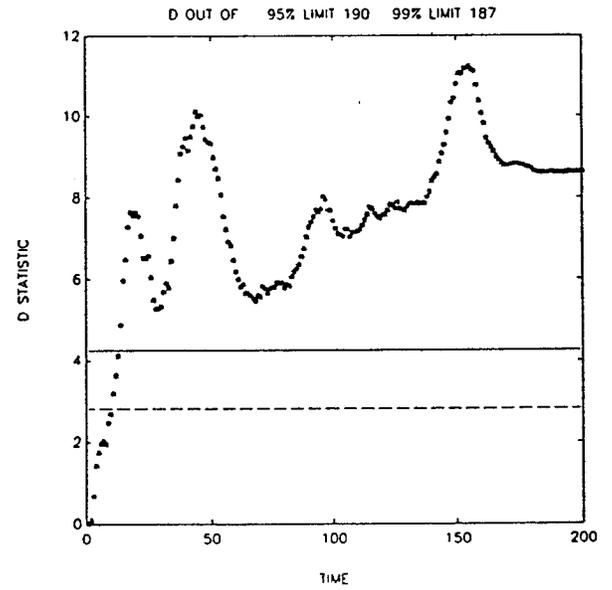
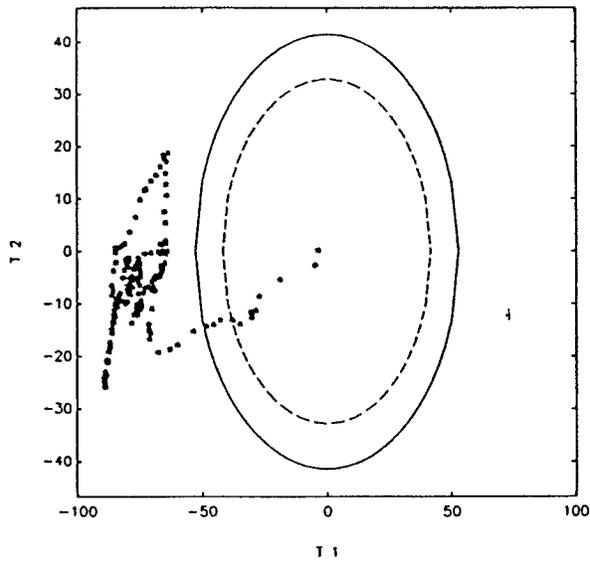
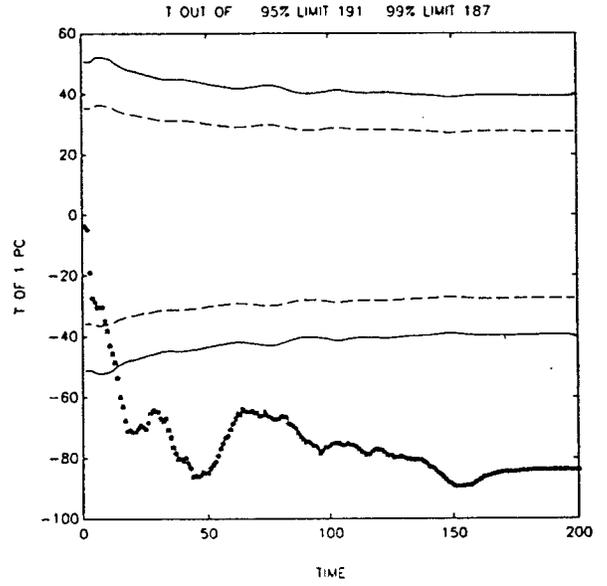
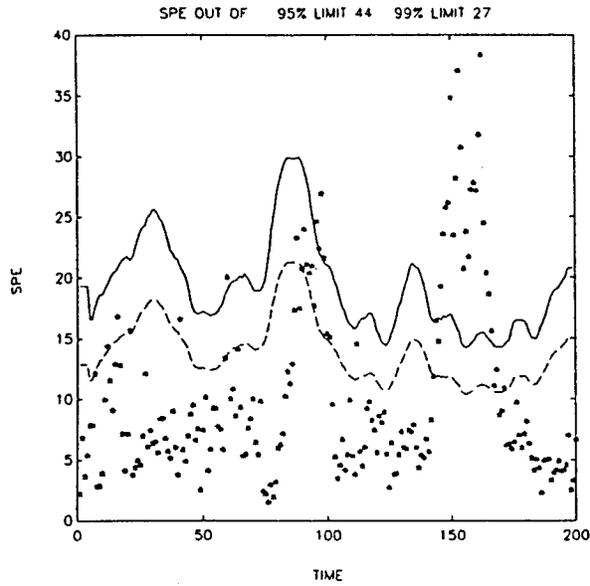
We will denote the lifted vector at time  $t$  with missing future measurements filled in as  $\hat{\mathcal{Y}}_t(j)$ , where  $t$  and  $j$  denote the time and batch index.

- For each time step, the confidence limits for the SPE and P.C.'s can be established.
- Now, at each time step for each batch, compute the P.C.s and SPE and compare against the confidence intervals.

# Good Batch



# Bad Batch I



# Bad Batch II

